

2.3 Adaptive Kontrolle (Optimalsteuerung)

$$\dot{\underline{x}} = f(\underline{x}, \underline{u}, t) \quad \underline{x} \in \mathbb{C}^n \quad \text{Zustandsvektor}$$

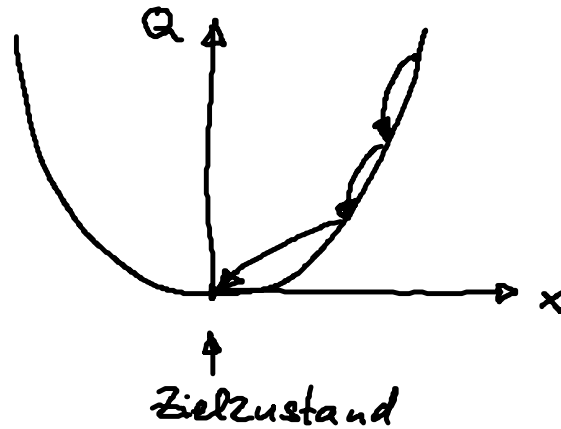
$$\underline{u} \in \mathbb{C}^m \quad \text{Kontrollpar. (input)}$$

Kostenfunktion $Q(\underline{x}(t), t)$ minimalisieren!
(cost fct., goal fct.)

$$Q \geq 0$$

$$\lim_{t \rightarrow \infty} Q(\underline{x}(t), t) = 0$$

\Rightarrow finde $\underline{u}(t)$



Speed gradient method

A. Fradkov, Miroshnik, Nikiiforov: Nonlinear and Adaptive Control of Complex Systems (Kluwer, Dordrecht 1999)
A. Fradkov: Cybernetical Physics: From Control of Chaos to Quantum Control (Springer 2007)

speed of Q : $\dot{Q} = \frac{\partial Q}{\partial t} + \nabla_{\underline{x}} Q(\underline{x}, t) \dot{\underline{x}}$

\uparrow \uparrow $\stackrel{=}{=} f(\underline{x}, \underline{u}, t)$
 hängt nicht von u ab

$$\dot{\underline{u}} = -\Gamma \nabla_{\underline{u}} \dot{Q}$$

Richtung im u -Raum, in der \dot{Q} am stärksten abnimmt

$$\Rightarrow \dot{Q} < 0 \quad \Rightarrow Q \text{ nimmt ab} \quad \Rightarrow Q \rightarrow 0 \quad t \rightarrow \infty$$

Anwendung: selbstadaptive Kontrolle der Rückkopplungsstärke K bei zeitverzög. Rückkopplung ($K \hat{=} u$)

- unbekannte oder driftende Systemparameter
Lehnert, Hövel, Flunbert, Guzenko, Trachow, Schöll :

Chaos 21, 043111 (Okt. 2011)

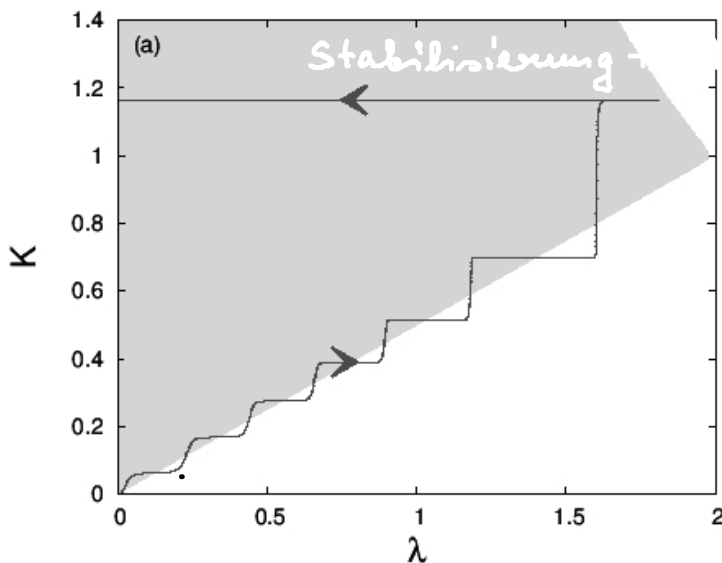
Stabilisierung eines Fixpunktes:

$$\begin{aligned} \dot{x} &= \lambda x + \omega y - K [x(t) - x(t-\tau)] & \lambda > 0 \\ \dot{y} &= -\omega x + \lambda y - K [y(t) - y(t-\tau)] & \text{Bif. par.} \end{aligned}$$

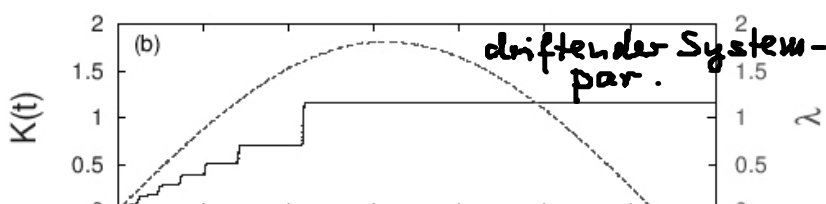
Fixpt. $x^* = y^* = 0$, Eigenwerte ($K=0$) $\lambda \pm i\omega$
 \Rightarrow inst. Fokus ($\lambda > 0$)

Kostenfkt. $Q = \frac{1}{2} [(x(t) - x(t-\tau))^2 + (y(t) - y(t-\tau))^2]$

$$\begin{aligned} \dot{K} &= -\Gamma \frac{\partial \dot{Q}}{\partial K} = -\Gamma \left\{ [x(t) - x(t-\tau)] \frac{\partial}{\partial K} [\dot{x}(t) - \dot{x}(t-\tau)] \right. \\ &\quad \left. + [y(t) - y(t-\tau)] \frac{\partial}{\partial K} [\dot{y}(t) - \dot{y}(t-\tau)] \right\} \\ &= \Gamma \left\{ [x(t) - x(t-\tau)] [(x(t) - x(t-\tau)) - (x(t-\tau) - x(t-2\tau))] \right. \\ &\quad \left. + [y(t) - y(t-\tau)] [(y(t) - y(t-\tau)) - (y(t-\tau) - y(t-2\tau))] \right\} \\ &= \Gamma \left\{ [x(t) - x(t-\tau)] [x(t) - 2x(t-\tau) + x(t-2\tau)] \right. \\ &\quad \left. + [y(t) - y(t-\tau)] [y(t) - 2y(t-\tau) + y(t-2\tau)] \right\} \end{aligned}$$

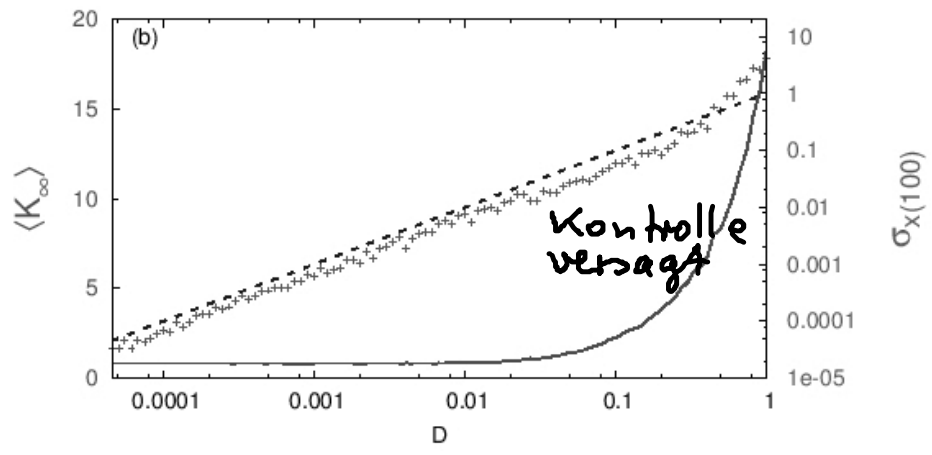
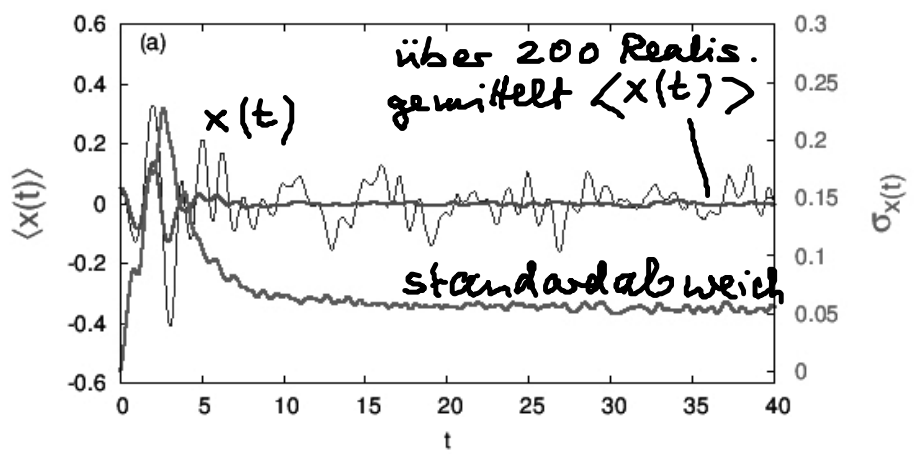


adaptive zeitverzögerte
Rückkopplungskontrolle
eines Fixpunktes
bei driftendem System-
parameter λ



0 500 1000 1500 2000 2500 3000 3500
t

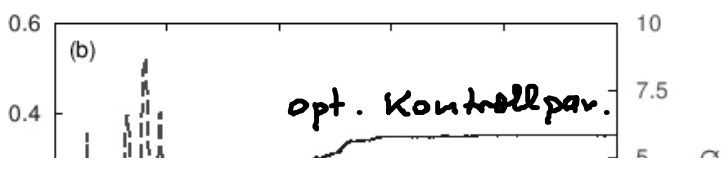
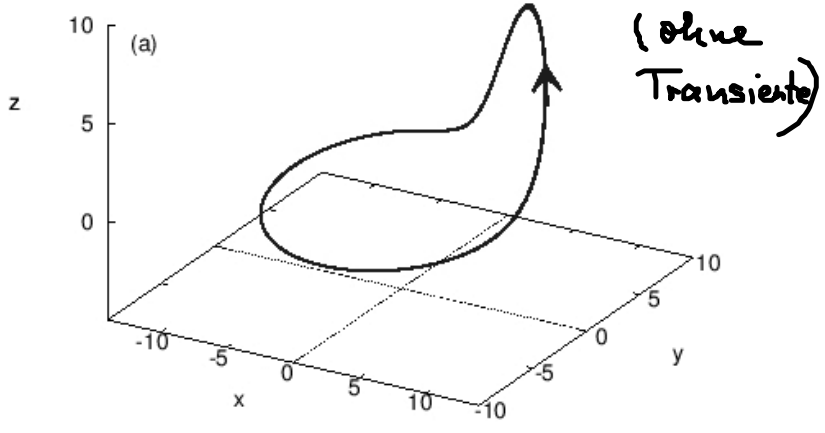
• robust gegen Rauschen $D\bar{x}_{1,2}(t)$:



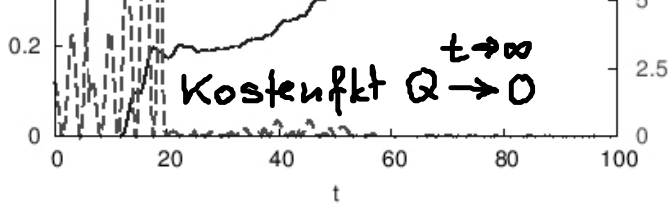
Stabilisierung eines instab. period. Orbits

Rössler - System (chaotisch)

instabiler period. Orbit stabilisiert



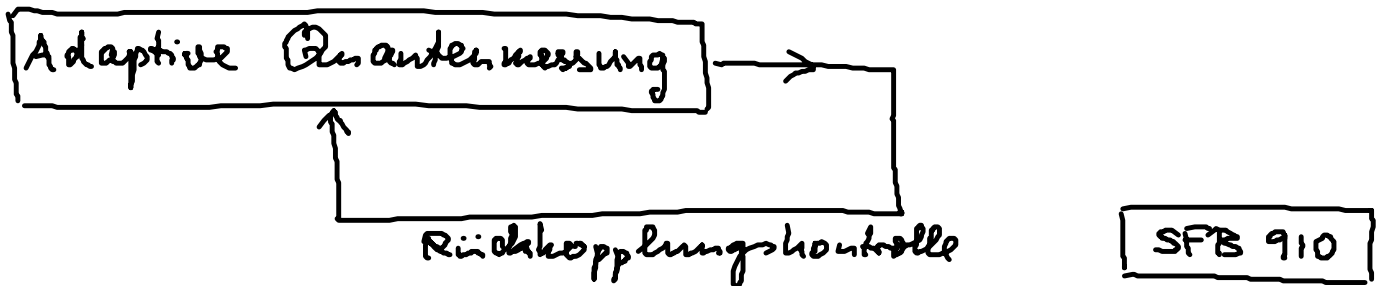
$$\tau = 5.9.. = T_{uro}$$



2.4 Quantenkontrolle

Howard Wiseman & G. Milburn: Quantum Measurement and Control (Cambridge U Press 2010)

5th Int. Conf. on Physics and Control (PhysCon 2011, Leon):
 "Bringing quantum jumps under control"



Vortrag H. Wiseman: TU Berlin, Mi 7.12.2011 16:00

"How many bits does it take ^{to track} an open quantum system"

R. Kosloff & H.M. Wiseman: PRL 106, 020406 (2011)