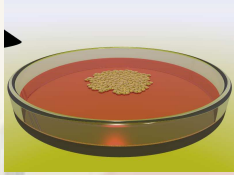


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## Introduction

### Simulation of cell-populations

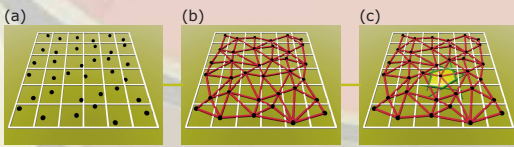


- Detailed understanding of the basic mechanisms that determine cell population growth is an active field of research; Particularly in-vitro experiments constitute an important and successful investigation tool, since the growth conditions can be varied in a wide range
- By definition of models one can study specific mechanisms neglecting unknown influences in experiments
- Detailed off-lattice models and lattice models exist [1,2] however lattice models are more promising to reduce the computational demand but might generate lattice artefacts.
- Single-cell-based models allow for the consideration of cellular heterogeneity, spatio-temporal fluctuations of the interface between cell population and growth medium and intracellular regulation mechanisms.

→ Necessity of: Fast Simulation tool combining advantages of off-lattice models (no lattice symmetry) with computing speed of lattice models.

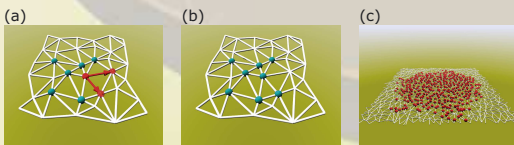
## Model

### Concept of unstructured lattice



- Random distribution of Voronoi Points on a square lattice by setting exactly one point to each square (a)
- Define neighbors by a **Delauney Triangulation** (b)
- Corresponding cells are accessible by the dual graph of Delauney diagram, the **Voronoi diagram** (c)

### Kinetic Monte Carlo Simulation



(1) time increment

$$\Delta t = \frac{\ln(1 - \xi)}{\sum_i p_{i \rightarrow j}}$$

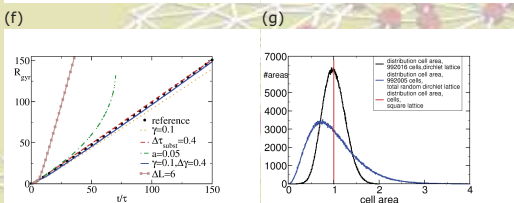
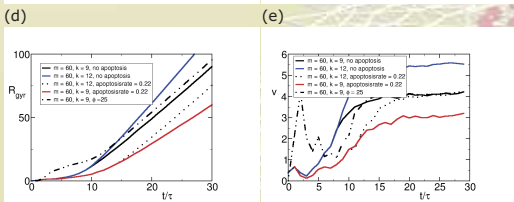
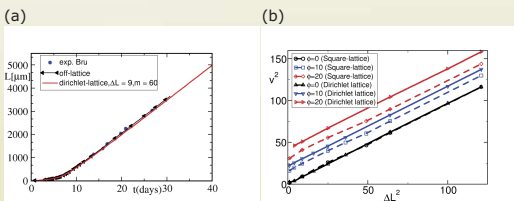
(2) Gyration radius

$$R_{gyr} = \sqrt{\frac{1}{N} \sum_{i=1}^N (L_i - R_{cm})^2}$$

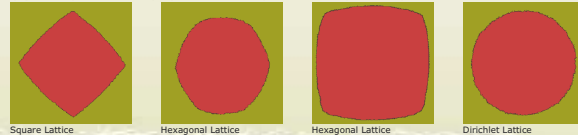
- Definition of probabilities for basic processes by average rates of migration  $\phi$  and cellular division  $\lambda = 1/\tau$  with cell-cycle times  $\tau$ , every single state is defined by all possible changes in configurational space
- **Stepwise random selection** of possible changes (a), (b) generates the dynamics of cell population development with an increasing time  $\Delta t$  (1), resulting in a simulated population (c)
- Growth conditions now can be investigated by change of the initial parameters  $\phi$ ,  $\lambda$ ,  $k$  and  $m$  where  $k = \Delta R - 1$  is the proliferating rim at the border of the population and  $m$  is the control strength of the dispersion of cell-cycle distribution ( $m=1$  is Poissonian)
- Additional parameters define the possibility for cell-cycle mutation, transmitted from the mothercell and apoptosis as a third basic process

## Results

### Dynamics and Morphology



(c) Comparison of population shape for sharp cell-cycle distribution  $m \rightarrow \infty$



- **Biological interpretation:** Biomechanical form of contact inhibition determines qualitative growth regimes.
- Growth simulations with free diffusion satisfy the kinetic properties with a linear phase after an initial phase of exponential growth and agree with experiments (a)
- Expansion velocity increases with cell migration activity  $\phi$  (a), threshold for contact inhibition (via  $k$ ), and width of cycle time distribution (decreasing  $m$ )
- an underlying structure of standard lattices shows strong lattice effects, where the Voronoi-structure shows **no lattice artefacts** (b),(c).
- Apoptosis change the dynamics of the cell-population growth where different parameters of apoptosis, migration and proliferating rim can lead to the same expansion velocity with different initial phases (d),(e)
- Mutations affect expansion kinetics and shape of cell populations, apoptosis lead to a delay of this effect, but deactivate it (f),(e)
- Cell area distribution is a realistic in contrast to structured lattice approaches or total random distributions (g)

## Conclusion

### Summary

The presented Voronoi-lattice model can reproduce the dynamics of tumor cell population growth observed in experiments [4] and simulated [2, 3] by means of a Kinetic Monte Carlo method. We are able to identify the different basic mechanisms that change the specific morphologies and dynamics in experiments. Hence a detailed understanding of cell population growth mechanisms is achieved.

### References

[1] M. Block, D. Drasdo and E. Schöll, in preparation, 2006.  
 [2] D. Drasdo, Adv. Compl. Syst. 2 & 3, 285-318, 2005.  
 [3] D. Drasdo, S. Höhme and M. Block, submitted, 2006.  
 [4] Bru et al, Biophys. J. 85, 2948-2961, 2003.