

Theoretical Material Science: Exercise Sheet 13**Classroom exercise – be there and explore****Exercise 29** (optional points): *Dilute magnetic semiconductors*

Having a semiconducting material that is ferromagnetic at the same time could open up a new field of electronics (*spintronics*). Unfortunately, there are some small difficulties, like finding a ferromagnetic semiconductor with a Curie temperature above room temperature. But this should be an easy task for theory – right?

The system $(\text{Ga}_{1-x}\text{Mn}_x)\text{As}$ is perhaps the most studied ferromagnetic semiconductor material. The basic structure is zincblende. A few Ga atoms are replaced by Mn, with x between 2 % and 10 % in experiment. (For much more Mn, the material becomes unstable and forms a different structure.) The highest reported Curie temperature is $T_C=173$ K (for 8 % Mn).

- a) In GaAs, Mn substitutes a (formally) three-fold positive Ga ion. Consider an *isolated* Mn^{3+} ion. Which electronic occupation and spin state do you expect? Remind yourself of the crystal field splitting diagram of a Mn^{3+} ion in a tetrahedral environment. Draw the levels and their occupation.
- b) As theorists, we can easily introduce any amount of Mn and keep the zincblende structure. In a key paper on GaMnAs (Ohno *et al.* APL **69**, 363 (1996)), the lattice parameter for GaAs is given as $a_{\text{GaAs}}=5.66$ Å ($x=0$), and that for *hypothetical* zincblende MnAs $a_{\text{MnAs}}=5.98$ Å ($x=1$). Use Vegard's law to estimate lattice parameters for $x=0.25$, 0.125, and 0.03125.
- c) Use DFT-LDA to compute the total and the atom- and angular-momentum-resolved partial density of states for ferromagnetic $\text{Ga}_{0.75}\text{Mn}_{0.25}\text{As}$ in a cubic 8-atom unit cell at the lattice parameter found above. Where are the Mn d levels in relation to all other states? Is there a gap in any of the spin channels? How many occupied spin-up and spin-down Mn d -levels are there? What is the difference to the "simple" Mn^{3+} ion?
- d) $\text{Ga}_{0.75}\text{Mn}_{0.25}\text{As}$ is not quite "dilute". Using pre-computed results for a 64-atom cell ($\text{Ga}_{\frac{31}{32}}\text{Mn}_{\frac{1}{32}}\text{As}$), investigate if the results for the smaller supercell prevail.
- e) Write down a (classical) nearest-neighbour only interaction Hamiltonian for the simple cubic $\text{Ga}_{0.75}\text{Mn}_{0.25}\text{As}$ 8-atom supercell above. How many nearest neighbours are there? What would be the simplest antiferromagnetic state? (Draw.)
- f) Create a supercell geometry that can contain this antiferromagnetic ground state (16 atoms total). What type of primitive lattice do the lattice vectors define? Compute the total energy once for a ferromagnetic state and once for an antiferromagnetic state. What is the energy difference $E_{\text{FM}} - E_{\text{AFM}}$? Use the difference to compute the interaction parameter in your Hamiltonian.
- g) For the interaction parameter derived from task f), calculate the Curie temperature. For a simple cubic lattice and a classical nearest-neighbour Ising Hamiltonian $-J \sum_{\langle i,j \rangle} S_i S_j$ with $S_i = \pm 1$, Monte Carlo results give $k_B T_C = J/0.221654$. Do you think that this is the highest T_C that one can achieve?

Outlook: We have only really investigated T_C for a single arrangement of Mn atoms on the lattice. One question of real interest is, could we predict a specific Mn arrangement for which T_C would be highest? We do not have the time to do so in this exercise, but we have prepared a few more supercells in the outlook part to illustrate the idea. Take a look, while the (long) calculation of part f) is running.

Please turn over!→

- **Webpage of the lecture:**
http://www.itp.tu-berlin.de/menue/lehre/lv/ss12/wahlpflichtveranstaltungen/theoretische_festkoerperphysik_i_ii_theoretical_material_science/
http://th.fhi-berlin.mpg.de/sitesub/lectures/spring_2012/
- **Lecture:** Tue. & Wed., 10:00 h -12:00 h (sharp!) in room EW 203, TU Berlin
- **Exercise:** Wed., 14:00 h in room EW 229
- **Literature:**
 - Ashcroft, Mermin, David: Solid state physics, Saunders College, Philadelphia, 1981
 - Kittel: Quantum theory of solids, Wiley, New York, 1963
 - Ziman: Principles of the theory of solids, Cambridge University Press, Cambridge, 1964
 - Ibach, Lueth: Solid-state physics: an introduction to principles of materials science, Springer, Berlin, 1995
 - Madelung: Festkörpertheorie, Springer, Berlin, 1972
 - Scherz: Quantenmechanik, Teubner, Stuttgart, 1999
 - Dreizler, Gross: Density functional theory: an approach to the quantum many-body problem, Springer, Berlin, 1990
 - Parr, Yang: Density-functional theory of atoms and molecules, Oxford University Press, Oxford, 1994
 - Anderson: Basic notations of condensed matter physics, Benjamin/Cummings, London, 1984
 - Marder: Condensed matter physics, Wiley, New York, 2000
 - Martin: Electronic Structure, Cambridge University Press, Cambridge, 2004
 - Kohanoff: Electronic Structure Calculations for Solids and Molecules: Theory and Computational Methods, Cambridge University Press, Cambridge, 2006
- **"Übungsschein"-criteria:**
 - Regular and active participation in the exercises
 - Presentation of homework tasks and
 - 50% of the homework points.
 - Active participation in computational exercises
- **Consultation hours:**
 - Prof. Dr. Matthias Scheffler, Dr. Alex Tkatchenko, Dr. Patrick Rinke: by appointment
 - Dr. Volker Blum: Available Wed. 16:00 (after the exercise class) or by appointment